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Joint Work with Crystal C. Din, Einar B. Johnsen, Ka I Pun, S. Lizeth T. Tarifa



International ABS Workshop 2018, TU Darmstadt

[Invited Paper at Tableaux 2017, LNCS 10501, pp. 22–43]

Once Upon a Time in Darmstadt



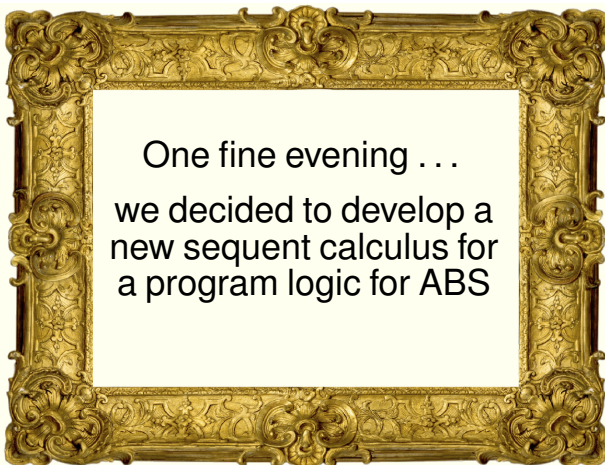
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Once Upon a Time in Darmstadt



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Would be Good to Have a Formal Semantics ...

- ... to guide the design of the calculus' rules
- ... to prove soundness and, eventually, completeness



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- ... to prove soundness and, eventually, completeness

Wanted: Trace Semantics for a Concurrent, Distributed Language

Given a program statement s and an initial state σ , the **semantics** of s is the set of all possible execution traces τ that are possible when s is started in σ

- ▶ **Trace**: a possibly empty, possibly infinite, sequence of execution states
- ▶ **Global semantics**: state holds set of processors, each with own heap
- ▶ Concurrent behavior dependent on scheduler: **set** of traces

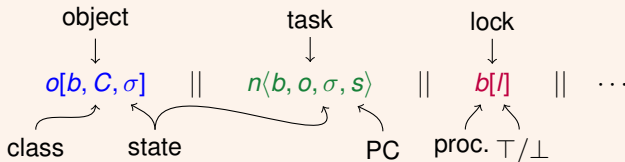
SOS: Structural Operational Semantics

Standard Approach in Programming Language Semantics



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Reduction rules pattern match on **runtime configurations** \sim states



Typical Reduction Rule: object creation:

$$\frac{n\langle b, o, \sigma, T \ z = \mathbf{new} \ C(v); s \rangle}{b'(\overline{T}) \ || \ n'\langle b', o', \sigma'_{init}, s_{task} \rangle \ || \ o'[b', C, \sigma_{init}] \ || \ n\langle b, o, \sigma, s\{z/o'\} \rangle}$$

where b', o', n' new; $\overline{T} f$; s' init block of c ; $\sigma_{init} = \overline{T} f$; $s_{task} = s' \{ \mathbf{this}/o'; \mathbf{suspend} \}$

A Clash



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What we Have

Programming Language: Structural operational semantics (SOS)

What we Need

Sequent Calculus: Model theoretic, denotational semantics

What's Wrong with SOS?



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SOS Rules Define Interpreter of Target Language

- ▶ Many rules, often 3–5 for each statement (> 60 for ABS)
- ▶ Not **modular**:
 - ▶ No separation between **local** and **global** computation
 - ▶ Next applicable rule depends on current configuration
 - ▶ Small rule modifications have unforeseeable **consequences**

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Program Logics Based on (forward / backward) **Symbolic Execution**

- ▶ Ill-matched to SOS
- ▶ **Better**: denotational semantics with model theoretic flavor

Ok, We Need a Denotational Semantics —So What?



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There is none! A least not for a complex, concurrent programming language

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KeY, Why, Dafny, but even Dijkstra, Hoare Calculus only

C, C++, Java, ABS SOS only

Concurrent separation logic Stephen Brookes' action traces

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Starting Point

Model theoretic semantics for while language in:

Richard Bubel, Crystal Chang Din, Reiner Hähnle, Keiko Nakata.

A Dynamic Logic with Traces and Coinduction. TABLEAUX 2015: 307-322

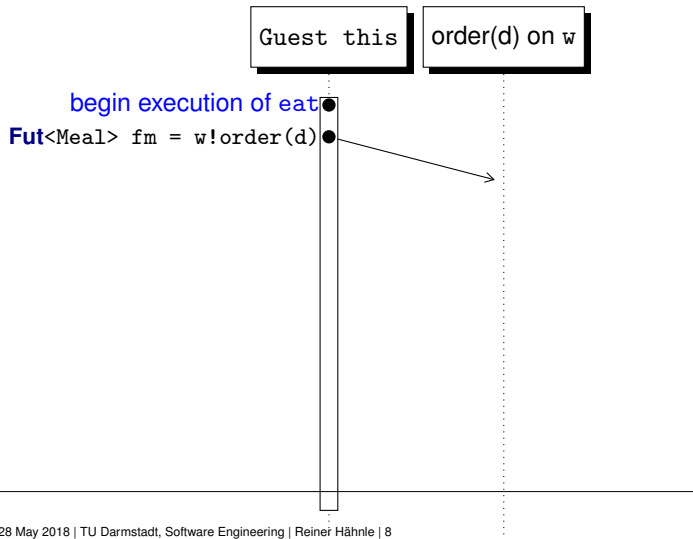
ABS Communication Structure



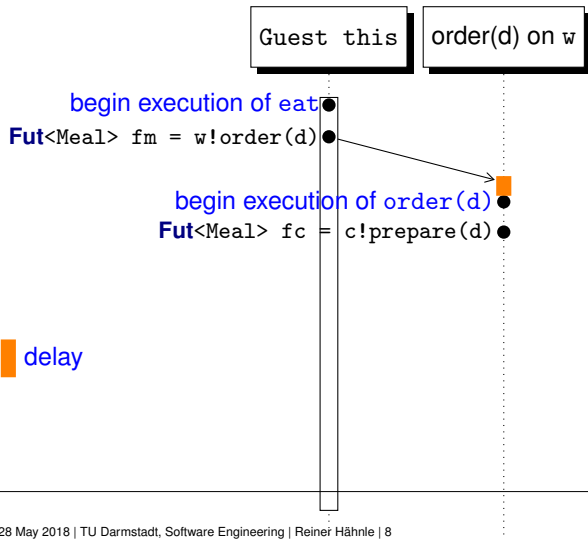
Guest this

begin execution of eat

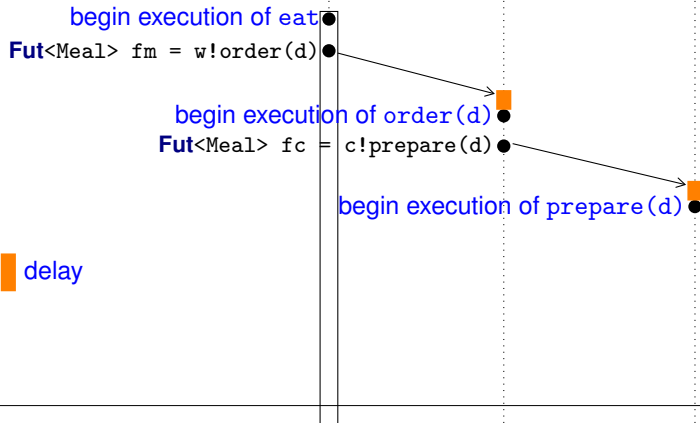
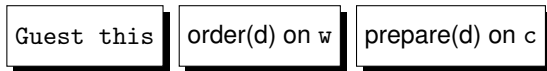
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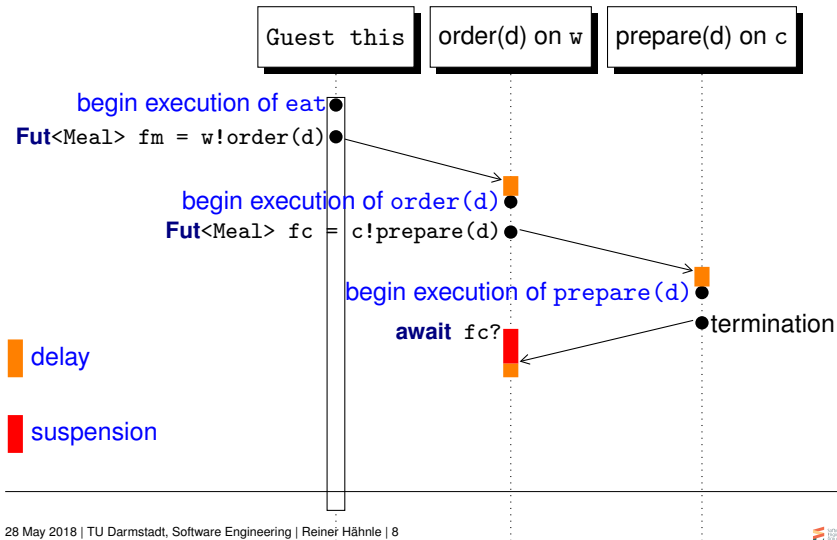
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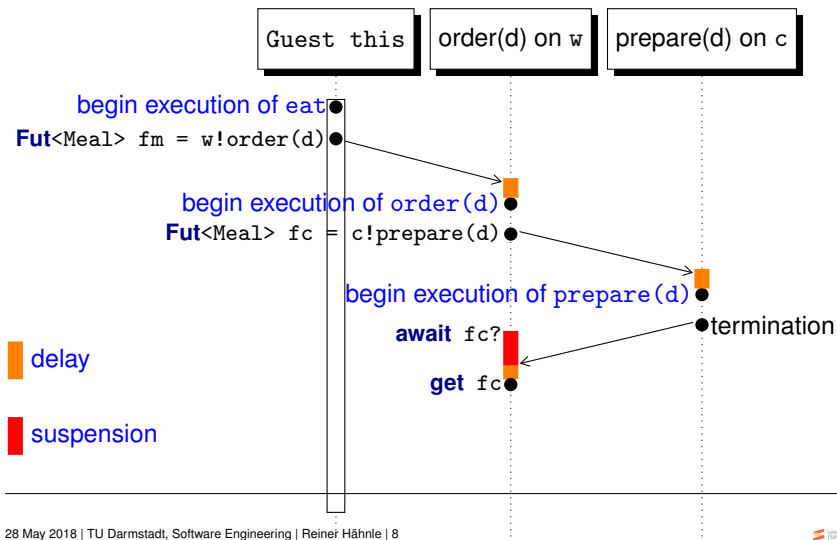
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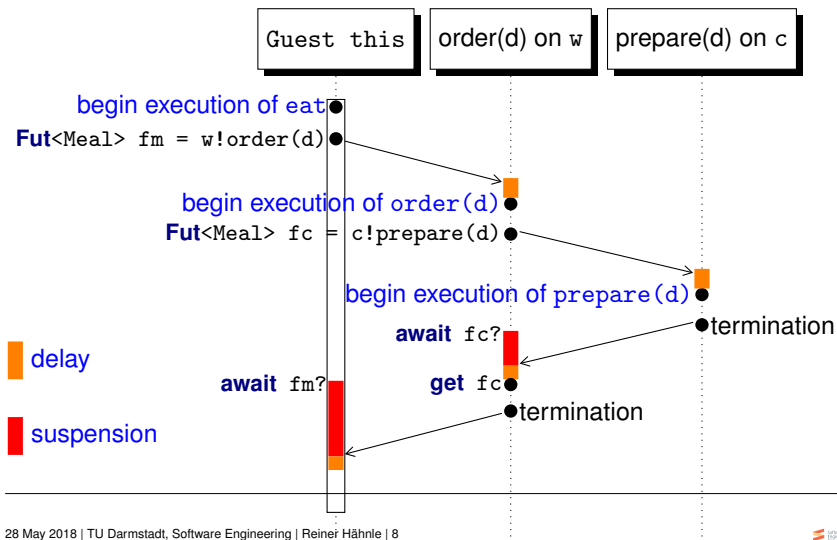
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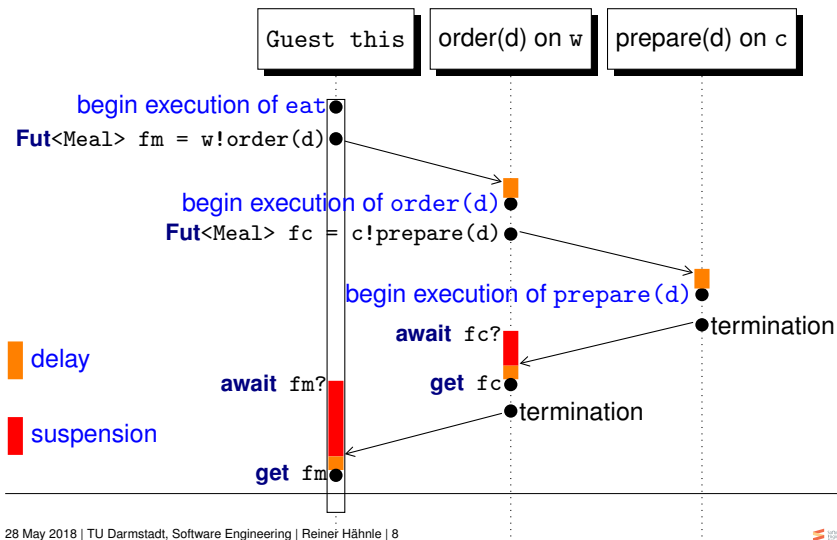
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ABS Communication Structure



ABS Communication Structure





Given an ABS statement, compute all possible finite or infinite traces

... in the following manner:

Local — for given initial state, current object **this**, heap, future **destiny**

Modular — evaluation of one statement does not depend on others'

Composable — obtain global behavior by composition of object-local behavior

A Denotational Semantics for ABS



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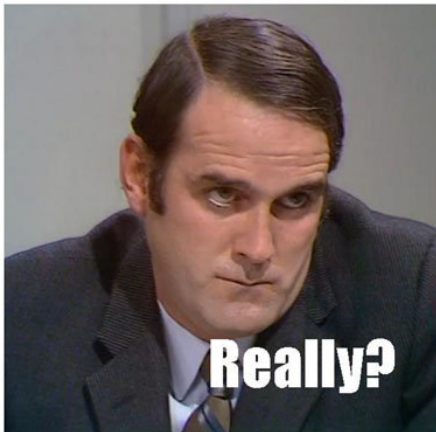
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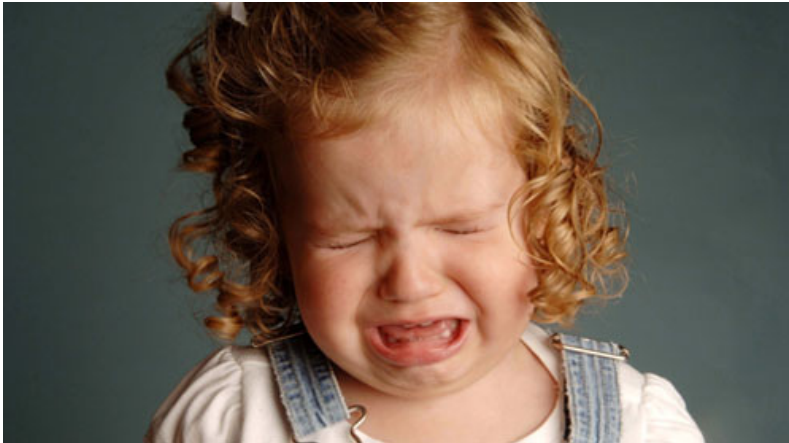
$v = f.\text{get}; \text{ if } (v == 0) \text{ then } o.m() \text{ else await } f'?$

- ▶ Behavior depends on whether f, f' resolved (starvation, blocking!)
- ▶ Conditional depends on value v from previous asynchronous call
- ▶ Execution of m requires value of o

Despair? Sit Down and Cry?



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No!

Boldly Go where no Semantics has Gone Before



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Abstract away from Unknowables during Semantic Evaluation

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Generate all—**cumulative semantics**—with appropriate **path condition**

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Use **symbolic values**: inspired by **symbolic execution**

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Generate all—**cumulative semantics**—with appropriate **path condition**
- ▶ Don't know values of parameters, attributes, initial state —
Use **symbolic values**: inspired by **symbolic execution**
- ▶ Don't know identity of **this**, **destiny** —
Render semantic evaluation **parametric** in current object, future



Definition (Semantic Evaluation)

For each object O , future F , ABS statement s , **symbolic** state σ

$$\text{val}_{\sigma}^{O,F}(s)$$

is a **semantic evaluation** function yielding a set of **symbolic traces** starting in σ .



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Definition (Path Condition, Symbolic Trace)

A **path condition** pc is a set of quantifier-free formulas over $\text{Exp}(\mathcal{L})$, where \mathcal{L} are memory locations (variables) and $\text{Exp}(\mathcal{L})$ ABS expressions over \mathcal{L} .

A (conditioned) **symbolic trace** has the form $pc \triangleright \tau$, where τ is a finite or infinite sequence of symbolic states.



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Definition (Symbolic State)

A **symbolic state** is a function $\sigma : \mathcal{L} \rightarrow \text{Exp}(\mathcal{L})$.

Symbolic Traces

Conventions, Notation, Example



- ▶ Assume $\sigma(\ell) \in \text{Exp}(\mathcal{L})$ is always fully evaluated
 \Rightarrow if $\sigma(\ell)$ contains no symbol from \mathcal{L} then $\sigma(\ell) \in D$
- ▶ Likewise, symbol-free path condition is either “true” or “false”
- ▶ Identify $\text{true} \triangleright \tau$ with τ
- ▶ Extend trace with single successor state: $\tau \curvearrowright \sigma$
- ▶ Lifting states to singleton traces: $\langle \sigma \rangle$
- ▶ Denote $\sigma(\ell) = e$ with $\ell \mapsto e$

$$\{(v_y \neq 0)\} \triangleright \langle [O.i \mapsto v_0, y \mapsto v_y, l \mapsto v_1] \rangle \curvearrowright [O.i \mapsto 42, y \mapsto v_0 + v_y, l \mapsto v_1]$$

- ▶ **Empty trace** denoted ε
- ▶ **Concatenation** of traces $\tau \cdot \omega$ (only defined if τ finite)

And Now ... Let's Go!



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Local Semantics of ABS

Block Scopes



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Scopes

ABS has block statements that define variable **scopes**: $\{s\}$, where s a statement

Evaluation of block scopes **without local variable declarations**

$$\text{val}_{\sigma}^{O,F}(\{s\}) =$$

Local Semantics of ABS

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Local Semantics of ABS

Skip and Local Variable Assignment



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$$\text{val}_\sigma^{O,F}(\mathbf{skip}) = \{\emptyset \triangleright \langle \sigma \rangle\}$$

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Lätt som en plätt!

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Local Semantics of ABS

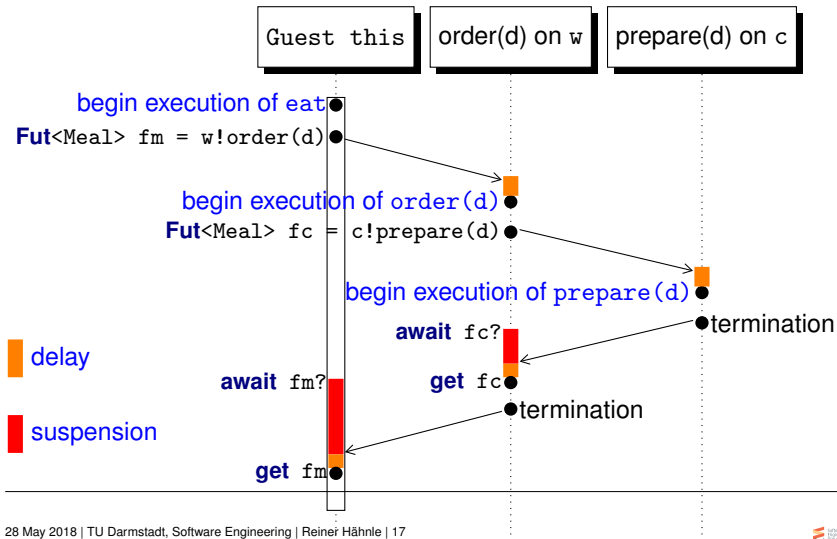
Skip and Local Variable Assignment



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Recall the ABS Communication Structure





Lifting Event Markers to Traces

Let $ev(\bar{v})$ be an **event marker** with arguments \bar{v}

How to associate $ev(\bar{v})$ with a state σ inside a trace τ ?

$$ev_{\sigma}(\bar{v}) = \langle \sigma \rangle \curvearrowright ev(\bar{v}) \curvearrowright \sigma$$

- ▶ **Event trace** $ev_{\sigma}(\bar{v})$ is a trace of length 3
- ▶ **Advantage:** Traces begin and end always with states



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Event markers will be used to ensure **well-formedness** of traces:
objects must be created before they can be accessed, etc.

Local Semantics of ABS

Object Creation



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```
class  $C(\bar{T} \ \bar{a})$  implements  $I$  { ... }  
 $\ell = \mathbf{new} \ C(\bar{e});$  // create new object of class  $C$   
                    // with class attribute arguments  $\bar{e}$  and assign to  $\ell$ 
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Local Semantics of ABS

Object Creation



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class C( $\bar{T}$   $\bar{a}$ ) implements I { ... }  
 $\ell$  = new C( $\bar{e}$ ); // create new object of class C  
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Object Initialization

- ▶ Wlog no initialization block

$$\text{val}_{\sigma}^{O,F}(\ell = \text{new } C(\bar{e})) =$$

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sets each attribute to fresh symbol, class attributes to constructor values \bar{v}

$$\text{val}_{\sigma}^{O,F}(\ell = \text{new } C(\bar{e})) =$$
$$\text{isFresh}(o), \text{class}(o) = C, \sigma' = C.\epsilon(o, \bar{v}) \circ \sigma,$$
$$\bar{v} = \text{val}_{\sigma}^{O,F}(\bar{e})$$

Local Semantics of ABS Object Creation



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sets each attribute to fresh symbol, class attributes to constructor values \bar{v}
- ▶ Event marker **$\text{newEv}_\sigma(\text{this}, \text{newObject}, \text{attributeValues})$**

$$\text{val}_\sigma^{O,F}(\ell = \text{new } C(\bar{e})) = \{pc \triangleright \text{newEv}_\sigma(O, o, \bar{v}) \cdot \tau \mid$$
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Local Semantics of ABS

Asynchronous Method Call



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$l = e'!m(\bar{e});$ // asynchronous call of m on e' with arguments \bar{e}
// assign result to l

Local Semantics of ABS

Asynchronous Method Call



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Event Marker

Invocation event $invEv_{\sigma}(caller, callee, future, method, args)$

Local Semantics of ABS Asynchronous Method Call



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What is “**” ?

The “Chop” Constructor for Traces



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Semantics of the Sequencing Statement in Terms of Traces

$r; s$

The “Chop” Constructor for Traces



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Semantics of the Sequencing Statement in Terms of Traces

$r; s$

$\underbrace{\sigma_0 \cdots \sigma_n}_r$

$\underbrace{\sigma_n \sigma_{n+1} \cdots}_s$

The “Chop” Constructor for Traces



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Semantics of the Sequencing Statement in Terms of Traces

$r; s$

$$\underbrace{\sigma_0 \cdots \sigma_n}_r \quad ** \quad \underbrace{\sigma_n \sigma_{n+1} \cdots}_s$$

- ▶ $\tau \underline{**} \tau'$ is “chop” on traces: cut out one redundant state

The “Chop” Constructor for Traces



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Semantics of the Sequencing Statement in Terms of Traces

$$\begin{array}{ccc} & r; s & \\ & \parallel & \\ \underbrace{\sigma_0 \cdots \sigma_n}_r & \underline{**} & \underbrace{\sigma_n \sigma_{n+1} \cdots}_s \end{array}$$

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$$\begin{array}{c} r; s \\ \underbrace{\hspace{10em}} \\ \sigma_0 \cdots \sigma_n \sigma_{n+1} \cdots \\ \parallel \\ \underbrace{\sigma_0 \cdots \sigma_n}_r \quad ** \quad \underbrace{\sigma_n \sigma_{n+1} \cdots}_s \end{array}$$

- ▶ $\tau ** \tau'$ is “chop” on traces: cut out one redundant state
- ▶ If τ is infinite, returns τ , otherwise defined as above



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$$\begin{array}{c} r; s \\ \underbrace{\qquad\qquad\qquad}_{\sigma_0 \cdots \sigma_n \sigma_{n+1} \cdots} \\ \parallel \\ \underbrace{\sigma_0 \cdots \sigma_n}_r \quad \underbrace{**}_{\sigma_n \sigma_{n+1} \cdots} \end{array}$$

- ▶ $\tau \underline{**} \tau'$ is “chop” on traces: cut out one redundant state
- ▶ If τ is infinite, returns τ , otherwise defined as above
- ▶ Event lifting $ev_\sigma(\bar{v}) = \langle \sigma \rangle \curvearrowright ev(\bar{v}) \curvearrowright \sigma$: events are “choppable”

Local Semantics of ABS

Method Execution



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Event Marker

Invocation **reaction** event $invREv_{\sigma}(caller, callee, future, method, args)$

$$\text{val}_{\sigma}^{O,F}(C.m) =$$

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$$\text{lookup}(m, C) = T m(\bar{T} \bar{\ell}')\{s\},$$

- ▶ Unknown parameter values initialized with fresh symbolic constants \bar{v}_0
- ▶ Call parameters inside scope: no name clash

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Method Execution



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- ▶ Unknown parameter values initialized with fresh symbolic constants \bar{v}_0
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- ▶ Unknown caller initialized with fresh parameter O'

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Conditional, method return, synchronous calls: straightforward

Local Semantics of ABS

Method Execution



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Event Marker

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Local Semantics of ABS Method Execution



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Event Marker

Invocation reaction ev

$\text{val}_{\sigma}^{O,F}(C,m)$

- ▶ Unknown parameter
- ▶ Call parameters
- ▶ Unknown caller

Conditiona



d, args

$\text{resh}(O', \bar{v}_0)$

constants \bar{v}_0

lightforward



Problems with Release of Control and Interleaving

1. Impossible to know the computation **state after resumption**
2. When composing behavior, we need to know **interleaving points**

$$\text{val}_{\sigma}^{O,F}(\text{suspend}) =$$



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Make use of **release events** and **continuations**

$$\text{val}_{\sigma}^{O,F}(\text{suspend}) = \{\emptyset \triangleright \text{relEv}_{\sigma}(O) \cdot \text{relCont}(O, F, \text{skip})\}$$

- *relCont* is not state/event, but **continuation marker** to store future behavior



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$$\text{val}_{\sigma}^{O,F}(\text{suspend}) = \{\emptyset \triangleright \text{relEv}_{\sigma}(O) \cdot \text{starve}(O)\} \cup \{\emptyset \triangleright \text{relEv}_{\sigma}(O) \cdot \text{relCont}(O, F, \text{skip})\}$$

- ▶ *relCont* is not state/event, but **continuation marker** to store future behavior
- ▶ Process might never be re-scheduled: causes different global behavior **starvation marker** (only at end of a trace) signifies this
- ▶ Continuation and starvation markers are not part of trace

Semantics of Sequential Composition — Continuation Passing Style



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In a **local** semantics, sequential composition becomes tricky

$$\text{val}_{\sigma}^{O,F}(r; s) =$$

Semantics of Sequential Composition — Continuation Passing Style



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In a **local** semantics, sequential composition becomes tricky

$$\text{val}_{\sigma}^{O,F}(r; s) =$$
$$\left\{ (pc_r \triangleright \tau_r) \mathbf{**} (pc_s \triangleright \omega_s) \mid pc_r \triangleright \tau_r \in \text{val}_{\sigma}^{O,F}(r), pc_s \triangleright \omega_s \in \text{val}_{\sigma'}^{O,F}(s), \right.$$
$$\left. \text{where } \sigma' = \text{last}(\tau_r) \text{ if } \tau_r \text{ is finite} \right\}$$

Semantics of Sequential Composition — Continuation Passing Style



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- ▶ **Non-termination**, **starving** handled in definition of ******: throw away ω_s

Semantics of Sequential Composition — Continuation Passing Style



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- ▶ r may contain **release points**

$\text{val}_{\sigma}^{O,F}(r; s) =$

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where $\sigma' = \text{last}(\tau_r)$ if τ_r is finite, arbitrary otherwise $\} \cup$

$\{pc_r \triangleright \tau_r \cdot \text{relCont}(O, F, r'; s) \mid pc_r \triangleright \tau_r \cdot \text{relCont}(O, F, r') \in \text{val}_\sigma^{O,F}(r)\}$

- ▶ **Non-termination**, **starving** handled in definition of ******: throw away ω_s
- ▶ τ_r must end with continuation marker: compose with s

Semantic Evaluation of Sequential Composition

Example



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$$\text{val}_{\sigma}^{O,F}(\text{suspend}; s) \stackrel{?}{=}$$

Semantic Evaluation of Sequential Composition

Example



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$$\text{val}_{\sigma}^{O,F}(\text{suspend}; s) \stackrel{?}{=}$$

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Semantic Evaluation of Sequential Composition

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Computation of Local Traces

Example



```
Int n() {  
  Int y = 10;  
  Fut<Int> f = 0;  
  f = this.m();  
  if (y == 0) then y = this.m() else await f; fi;  
  y = this.i + y;  
  return y;  
}
```

$$\text{val}_{C.\epsilon(O)}^{O,F}(C.n) = \{$$

$$\}$$

Computation of Local Traces

Example



```
Int n() {  
  Int y = 10;  
  Fut<Int> l = 0;  
  l = this!m();  
  if (y == 0) then y = this.m() else await l? fi;  
  y = this.i + y;  
  return y;  
}
```

$\text{val}_{C.\epsilon(O)}^{O,F}(C.n) = \{$
 $\{(10 = 0)\} \triangleright \langle [O.i \mapsto v_i] \rangle \curvearrowright \text{invREV}(O', O, F, n, _) \curvearrowright \dots$ **infeasible path condition**
 $\}$

Computation of Local Traces

Example



```
Int n() {  
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  l = this.m();  
  if (y == 0) then y = this.m() else await l? fi;  
  y = this.i + y;  
  return y;  
}
```

$$\text{val}_{C, \epsilon(O)}^{O, F}(C.n) = \{$$
$$\{(10 \neq 0)\} \triangleright \langle [O.i \mapsto v_i] \rangle \rightsquigarrow \text{invREv}(O', O, F, n, _) \rightsquigarrow \dots$$
$$\rightsquigarrow \text{futEv}(O, F, v_i + 10) \rightsquigarrow [O.i \mapsto v_i, y' \mapsto v_i + 10, l' \mapsto f_0]$$
$$\}$$

- Future f_0 in l already resolved at **await**: n runs to completion

Computation of Local Traces

Example



```
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$$\}$$

► n starves at **await**

Computation of Local Traces

Example



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$$\text{val}_{C \in (O)}^{O, F}(C.n) = \{$$
$$\{(10 \neq 0)\} \triangleright \langle [O.i \mapsto v_i] \rangle \rightsquigarrow \dots \rightsquigarrow \text{relEv}(O, f_0) \rightsquigarrow [O.i \mapsto v_i, y' \mapsto 10, l' \mapsto f_0]$$
$$\cdot \text{relCont}(O, F, \text{await } l'?; y' = \text{this.i} + y'; \text{return } y');$$
$$\}$$

- ▶ Release control at **await**: put remaining code in continuation

From Local to Global Traces



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Goal

Given a **main block** $\{\bar{T} \bar{\ell} = \bar{v}; s\}$ and ABS program P
produce all **valid, concrete** system traces

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1. Compute **local** traces of **main block**: $\mathcal{M} = \text{val}_{\epsilon}^{\text{Main}, f_0}(\{\bar{T} \bar{\ell} = \bar{v}; s\})$



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Result: initial **concrete**, non-empty traces with path condition true or false



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Result: initial **concrete**, **non-empty** traces with **path condition true or false**

2. Compute **local** traces of each **method** for all objects and futures:

$$\mathcal{G} = \{\text{val}_{C.\epsilon(O)}^{O,F}(C.m) \mid \text{class}(O) = C, m \in \text{mtd}(C), O \in \mathcal{O}, F \in \mathcal{F}, C \in P\}$$

3. Pick an initial concrete trace with path condition true from \mathcal{M} and extend it with suitable instances from \mathcal{G} , repeat



Definition (Global Trace Composition Rule)

Let sh be a finite concrete trace and q a **pool** (queue) of sets of symbolic traces. A **global trace composition rule** has the form

$$\frac{\text{Conditions on } sh, q}{sh, q \rightarrow sh', q'}$$

- ▶ Any exhaustive application of global trace composition rules yields one valid, global system trace, possibly infinite
- ▶ Initial configuration is: $\varepsilon, \{\mathcal{M}\} \cup \mathcal{G}$



How to Preempt Local Execution?

ABS has no preemption . . .

Interleave execution on different processors with **interleaving events**



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Execute arbitrary finite local trace, then interleave other process



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Execute arbitrary finite local trace, then interleave other process

$\Omega \in q$ $object(\Omega) = O$ $pc \triangleright \tau \cdot \omega \in \Omega$ | get symbolic trace on an O from pool q

$sh, q \rightarrow sh$

, q'



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$\Omega \in q$ $object(\Omega) = O$ $pc \triangleright \tau \cdot \omega \in \Omega$
 $last(sh) = \sigma$

get symbolic trace on an O from pool q
get final **concrete** state σ from sh

$sh, q \rightarrow sh$

, q'



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$\Omega \in q$ $object(\Omega) = O$ $pc \triangleright \tau \cdot \omega \in \Omega$
 $last(sh) = \sigma$
 $\tau \neq \varepsilon$

get symbolic trace on an O from pool q
get final **concrete** state σ from sh
make some finite progress

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, q'



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$\tau \neq \varepsilon$

$\omega \notin \{\varepsilon, relCont(O, _, _), starve(O)\}$

get symbolic trace on an O from pool q

get final **concrete** state σ from sh

make some finite progress

don't finish execution on O

$sh, q \rightarrow sh$

$, q'$



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Execute arbitrary finite local trace, then interleave other process

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 $last(sh) = \sigma$
 $\tau \neq \varepsilon$
 $\omega \notin \{\varepsilon, relCont(O, _, _), starve(O)\}$
 $pc_\sigma = true$ $wf(sh \underline{**} \tau_\sigma)$

get symbolic trace on an O from pool q
get final **concrete** state σ from sh
make some finite progress
don't finish execution on O
 σ -instance of $pc \triangleright \tau$ feasible, well-formed

$sh, q \rightarrow sh \underline{**} \tau_\sigma, q'$



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Interleave execution on different processors with **interleaving events**

Execute arbitrary finite local trace, then interleave other process

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$last(sh) = \sigma$

$\tau \neq \varepsilon$

$\omega \notin \{\varepsilon, relCont(O, _, _), starve(O)\}$

$pc_\sigma = true$ $wf(sh \ast\ast \tau_\sigma)$

$q' = q \setminus \Omega \cup \{\emptyset \triangleright iIREV_{last(\tau)}(O) \cdot \omega\}$

get symbolic trace on an O from pool q

get final **concrete** state σ from sh

make some finite progress

don't finish execution on O

σ -instance of $pc \triangleright \tau$ feasible, well-formed

update pool, insert interleaving events

$sh, q \rightarrow sh \ast\ast \tau_\sigma \ast\ast iIREV_{last(\tau_\sigma)}(O), q'$

Other Global Trace Composition Rules



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1. External interleaving
2. Release
3. Continuation
4. Starvation
5. Blocking

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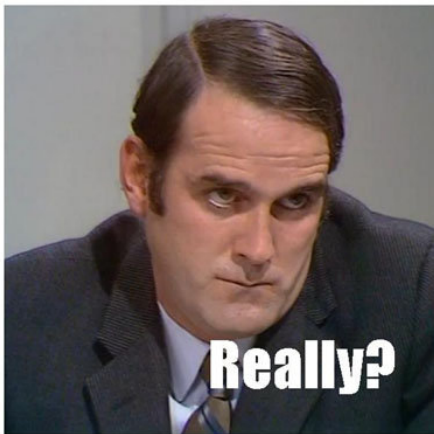


Other Global Trace Composition Rules



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Well-Formedness

Each global rule maintains well-formedness of trace extension: $wf(sh \underline{**} \tau_\sigma)$

- ▶ Needs to be checked only on finite, **concrete** traces
- ▶ Ensures that system **event sequence** is schedulable
- ▶ Predicate defined on **event structure** of given trace



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Examples of Well-Formedness Conditions

- ▶ “A release event for a future f cannot be preceded by a completion event for f ”
- ▶ “An external interleaving event on O must be directly followed by its corresponding interleaving reaction event”
 - ▶ This prevents **local preemption**

A Modular, Denotational Trace Semantics



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- ▶ Each statement is evaluated **locally** for any object, future
 - ▶ Evaluation of statement yields set of **symbolic traces**
 - ▶ Evaluation is **independent** from other statements

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 - ▶ Can characterize concurrency models via **well-formedness** by way of **dual** events
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One evaluation rule per statement, five global rules

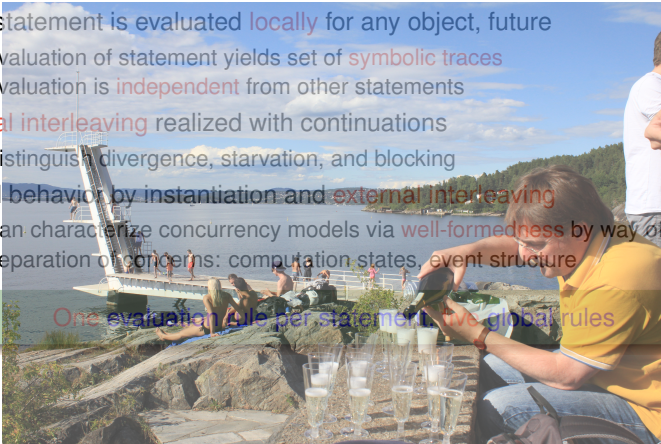
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 - ▶ Evaluation of statement yields set of **symbolic traces**
 - ▶ Evaluation is **independent** from other statements
- ▶ **Internal interleaving** realized with continuations
 - ▶ Distinguish divergence, starvation, and blocking
- ▶ Global behavior by instantiation and **external interleaving**
 - ▶ Can characterize concurrency models via **well-formedness** by way of **dual events**
 - ▶ Separation of concerns: computation states, event structure

One evaluation rule per statement, five global rules



A Modular, Denotational Trace Semantics



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Cheers!

One evaluation rule per statement, few global rules



Trace Formulas



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Symbolic Trace Formula

An (abstract) **symbolic trace formula** evaluates to a possibly infinite set of traces



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“Each time a router (= **this**) terminates the **getPk** method,”

`futEv(this,fr,getPk,_)`

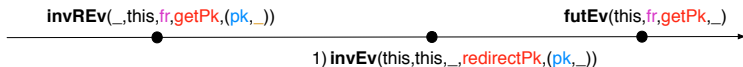




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“Each time a router terminates the **getPk** method, it must either have invoked a method to **redirect** a packet”

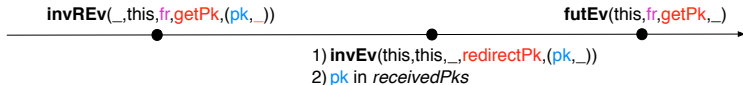




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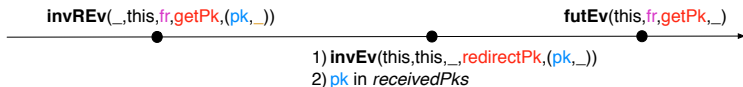
“Each time a router terminates the **getPk** method, it must either have invoked a method to **redirect** a packet or have stored that packet in its **receivedPks** set”



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Corresponding **symbolic trace formula**:

$$\omega_{fr,pk} \left(\text{invREv}(_,\text{this},fr,\text{getPk},(pk,_)) \ll \text{invEv}(\text{this},\text{this},_,\text{redirectPk},(pk,_)) \ll \text{futEv}(\text{this},fr,\text{getPk},_) \right) \vee \text{invREv}(_,\text{this},fr,\text{getPk},(pk,_)) \ll |pk \in \text{receivedPks}| \ll \text{futEv}(\text{this},fr,\text{getPk},_)$$



Definition (Trace Modality Formula)

1. Trace modality formulas **syntactically closed** under usual propositional and first-order operators.
2. If s is an ABS statement and Ψ a trace modality formula, then $\llbracket s \rrbracket \Psi$ is a trace modality formula.
3. If $\{u\}$ is an update and Ψ a trace modality formula, then $\{u\}\Psi$ is a trace modality formula.

Updates $\{\ell := exp\}$ or $\{ev(\bar{e})\}$ record state changes effected by assignments or the occurrence of communication events.



Definition (Evaluation of Trace Modality Formula)

Trace modality $\text{val}_\tau([\![s]\!] \Psi)$ is **true** if for any O, F :

If for each $\tau' \in \text{val}_{\text{last}(\tau)}^{O, F}(s)$ such that $\tau \underline{**} \tau'$ is well-formed $\text{val}_{\tau \underline{**} \tau'}^{O, F}(\Psi)$ holds.

“Any trace of s that extends τ is contained in Ψ ”

Semantics of Trace Modality Formulas



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With a semantics for trace modality formulas, we can start to design a calculus . . .

Asynchronous Method Call Semantics vs. Calculus



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Semantic Evaluation of Asynchronous Method Call

$$\text{val}_{\sigma}^{O,F}(\ell = e'!m(\bar{e})) = \{pc \triangleright \text{invEv}_{\sigma}(O, \text{val}_{\sigma}^{O,F}(e'), f, m, \text{val}_{\sigma}^{O,F}(\bar{e})) ** \tau \mid \\ \text{isFresh}(f), \text{method}(f) = m, pc \triangleright \tau \in \text{val}_{\sigma}^{O,F}(\ell = f)\}$$

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Sequent Rule for Asynchronous Method Call

$$\frac{\Gamma, \text{isFresh}(f) \Rightarrow \mathcal{U}\{\text{invEv}(\mathbf{this}, e', f, m, \bar{e})\}\{\ell := f\}[\mathbf{r}]\Psi}{\Gamma \Rightarrow \mathcal{U}[\ell = e'!m(\bar{e}); \mathbf{r}]\Psi}$$

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One-to-one correspondence between semantics and deduction rule!



Calculus

We have a sequent calculus for **local invariant** reasoning

- ▶ Turn into calculus for **global** reasoning (Richard)
- ▶ Generalize invariant into **contract**-based reasoning (Eduard)
- ▶ Formally prove **soundness**, possibly **completeness**
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Semantics

Apply semantic framework to other concurrent languages

- ▶ Related **active object** languages, e.g., MSR's Orleans
- ▶ C-like concurrent languages with **preemption**

Did You Notice the Oulipian Constraint?



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G. Perec